

gonal lattice¹⁰ while the calculated T_C - Q relation is for the cubic lattice. However in view of the small effects^{1,10,11} of the lattice transformation on the electronic properties of Nb_3Sn and V_3Si , we believe that the general T_C - Q behavior for the tetragonal lattice is similar.

Recently the temperature dependence of the pressure coefficient of the shear modulus of V_3Si was observed¹³ to decrease from a positive value to a negative minimum before reversing the sign back to positive at lower temperature. To explain this anomalous behavior and the negative dT_L/dP of V_3Si , it was proposed^{4,14} that the WLF model should be extended to include effects due to the pressure-induced interband charge transfer. By fitting the experimental data, Ting and Ganguly and Barsch and Rogowski found⁴ that pressure indeed enhances Q . Using Ting and Ganguly's estimate, we found that at 20 kbar Q increases by $\sim 10\%$ but still lies below Q_{CM} , in agreement with the observation of positive dT_C/dP at this pressure.¹⁵ According to this model, a pressure of ≥ 34 kbar is needed to raise Q to above Q_{CM} such that dT_C/dP changes to negative sign. Earlier it⁴ was determined through extrapolation that ~ 24 kbar is sufficient to stabilize the cubic lattice in V_3Si , suggesting that $Q_0 < Q_{CM}$, consistent with the recent observation of positive dT_C/dP for both the transforming and nontransforming V_3Si samples.¹⁶ On the other hand, Labbé, Barišić, and Friedel¹² obtained $Q_0 > Q_{CM}$.

This disagreement may be attributed to the uncertainties associated with the physical parameters used in their calculation. Lack of experimental data prevents us from making a similar comparison for Nb_3Sn . However a discussion of the experimental results at atmospheric pressure of doped Nb_3Sn in terms of the WLF model is worthwhile. For $\text{Nb}_3\text{Sn}_{1-x}\text{Al}_x$,¹⁷ a slight replacement of Sn by Al results in a decrease of Q and hence a decrease of T_L but an increase of T_C , as was observed. With large x , e.g., ≥ 0.08 , the lattice remains cubic below T_C , while T_C still increases. This absence of lattice transformation may arise from the higher density of imperfections in the crystal lattice, as for the case of V_3Si .¹⁸ However for $\text{Nb}_3\text{Sn}_{1-x}\text{Sb}_x$,¹⁹ the substitution of Sb for Sn not only increases Q but also changes the ratio c/a from < 1 to > 1 . The ratio Q_{LM}/Q_{CM} may consequently shift from > 1 to < 1 . The observed x -independent T_L and x -decreasing T_C are thus not unlikely. Studies of T_L and T_C of these samples under hydrostatic pressure, where presumably only Q variation is important, are planned to check the explanation of the doped- Nb_3Sn results, suggested above.

Recently Ting and Ganguly¹⁴ calculated the isothermal pressure coefficient $(\partial C_s/\partial P)_T$ of the shear modulus C_s , on the basis of the WLF model. By extending their formalism and using their notation, we have obtained an expression for dT_L/dP . T_L is defined as the temperature¹² at which the shear modulus C_s vanishes, i.e.,

$$C_s(T_L) = 0 = \frac{1}{2}Na^2q^2 \int_{-|E_0|}^{|E_0|} dE nE(f + E\partial f/\partial E) + C_s', \quad (1)$$

subject to the constraint

$$Q = \int_{-|E_0|}^{|E_0|} dE nf, \quad (2)$$

where $n = (4/\pi)[2|E_0|(|E_0| + E)]^{-1/2}$ is the density of states of the d sub-band; $f = [1 + \exp(E - E_F)/kT_L]^{-1}$, the Fermi function at T_L with Fermi energy E_F ; $3N$ is the number of transition metal atoms per unit volume; a is the interatomic distance, q the Slater coefficient of the atomic d orbital, $|E_0|$ the half-width of the d sub-band, and C_s' the temperature-independent part of C_s . Under pressure, with strain $\epsilon = \kappa P/3$, $N \rightarrow N(1 + 3\epsilon)$, $|E_0| \rightarrow |E_0|\exp(aq\epsilon)$, $a \rightarrow a(1 - \epsilon)$, $T_L \rightarrow T_L + (\partial T_L/\partial \epsilon)\epsilon$, and $Q \rightarrow Q + \delta Q$. By keeping only the first-order terms of ϵ in the Taylor's expansion of Eq. (1), we have

$$\frac{\partial \ln T_L}{\partial P} = + \frac{\frac{1}{6}N\kappa a^2 q^2 \int_{-|E_0|}^{|E_0|} dE nE[(1 + aq)f + (1 + 2aq)E\partial f/\partial E + (aqE - \partial E_F/\partial \epsilon)(\partial f/\partial E + E\partial^2 f/\partial E^2)] + \partial C_s'/\partial P}{\frac{1}{2}Na^2 q^2 \int_{-|E_0|}^{|E_0|} dE nE[(E - E_F)(\partial f/\partial E + E\partial^2 f/\partial E^2) + E\partial f/\partial E]}. \quad (3)$$

The term $\partial E_F/\partial \epsilon$ in Eq. (3) is determined by Eq. (2), allowing $Q \rightarrow Q + \delta Q$ under stress. It is interesting to note that the numerator can be identified with $(\partial C_s/\partial P)_{T_L}$ ¹⁴ and the denominator with $-T_L(\partial C_s/\partial T)_P$ provided $\partial E_F/\partial T$ is negligibly small. Hence Eq. (3) is reduced to the familiar

form $(\partial T_L/\partial P) = -(\partial C_s/\partial P)_{T_L}(\partial C_s/\partial T)_P^{-1}$ whose validity has been demonstrated for V_3Si .¹⁴ Lack of information about $\partial C_s/\partial P$ for Nb_3Sn makes the determination of δQ and consequently of $\partial E_F/\partial \epsilon$ very difficult. No attempt is made at using Eq.

(3) for any numerical calculation of $\partial T_L / \partial P$ for Nb_3Sn . A similar calculation on dT_C/dP , including the interband charge-transfer effect, can be done.

In conclusion, we have observed for the first time pressure-enhanced lattice transformation in a high- T_C superconductor. The opposite pressure effects on T_L and T_C of Nb_3Sn and V_3Si can be explained in terms of the WLF model by taking into account the pressure-induced interband charge transfer. Previous atmospheric results on T_L and T_C of doped Nb_3Sn samples were discussed and an expression for dT_L/dP was also obtained.

The author would like to thank Dr. L. R. Testardi for stimulating discussions throughout this work and Dr. L. J. Vieland for the sample. Valuable discussions with Dr. C. S. Ting and Professor G. R. Barsch are gratefully acknowledged.

*Research supported in part by National Science Foundation Grant No. GH-40866 and by the Research Corporation.

¹For a review see L. R. Testardi, in *Physical Acoustics*, edited by W. P. Mason and R. N. Thurston (Academic, New York, 1974), Vol. X.

²C. W. Chu and T. F. Smith, *Bull. Amer. Phys. Soc.* **17**, 311 (1972); T. F. Smith, R. N. Shelton, A. C. Lawson, and C. W. Chu, to be published.

³T. F. Smith, R. N. Shelton, and A. C. Lawson, *J. Phys. F: Metal Phys.* **3**, 2157 (1973).

⁴C. W. Chu and L. R. Testardi, *Phys. Rev. Lett.* **32**, 766 (1974).

⁵H. Neubauer, *Z. Phys.* **266**, 211 (1969); T. F. Smith, *J. Low Temp. Phys.* **6**, 171 (1972).

⁶C. W. Chu and G. S. Knapp, *Phys. Lett.* **46A**, 33 (1973).

⁷A. Sawaoka and N. Kawai, *Jpn. J. Appl. Phys.* **9**, 353 (1970).

⁸R. Mailfert, B. W. Batterman, and J. J. Hanak, *Phys. Status Solidi* **32**, K67 (1969); G. Shirane and J. D. Axe, *Phys. Rev. B* **4**, 2957 (1971).

⁹L. J. Vieland and A. W. Wicklund, *Solid State Commun.* **7**, 37 (1969).

¹⁰C. W. Chu and L. J. Vieland, to be published.

¹¹For a review see M. Weger and I. B. Goldberg, in *Solid State Physics*, edited by H. Ehrenreich, F. Seitz, and D. Turnbull (Academic, New York, 1974), Vol. 28.

¹²J. Labbé, S. Barišić, and J. Friedel, *Phys. Rev. Lett.* **19**, 1039 (1967); J. Labbé, *Phys. Rev.* **172**, 451 (1968).

¹³P. F. Carcia, G. R. Barsch, and L. R. Testardi, *Phys. Rev. Lett.* **27**, 944 (1971); P. F. Carcia and G. R. Barsch, to be published.

¹⁴C. S. Ting and A. K. Ganguly, *Phys. Rev. B* **9**, 2781 (1974); G. R. Barsch and D. A. Rogowski, to be published.

¹⁵T. F. Smith, *Phys. Rev. Lett.* **25**, 1483 (1970);

H. Neubauer, *Z. Phys.* **226**, 211 (1969).

¹⁶S. Huang and C. W. Chu, *Bull. Amer. Phys. Soc.* **19**, 228 (1974), and to be published.

¹⁷L. J. Vieland and A. W. Wicklund, *Phys. Lett.* **34A**, 43 (1971).

¹⁸S. J. Williamson, H. Fung, and C. S. Ting, *Phys. Rev. Lett.* **32**, 9 (1974).

¹⁹L. J. Vieland, *J. Phys. Chem. Solids* **31**, 1449 (1970).